## Abstract:

Given a set of \$n\$ vectors with \$d\$ dimensions, we consider a \$d \times n\$ matrix arranging them as column vectors. The matrix depends on the order of the column vectors, and we consider the {\em vector ranking problem} that finds the optimal permutation of column vectors to maximize/minimize an objective function defined by using non-decreasing subsequences of row vectors. The problem is a variant of mulit-dimensional sorting, and related to the Internet Reranking problems. We investigate the complexity of the problems, which depend on models to formulate the nondecreasingness.